

Strategy for sensing petal mode in presence of AO residual turbulence

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Pinna, Simone Esposito**

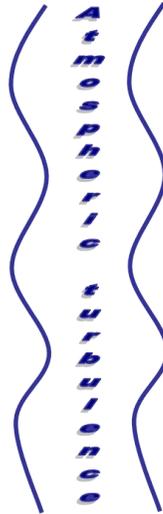
Adaptive Optics :

In space

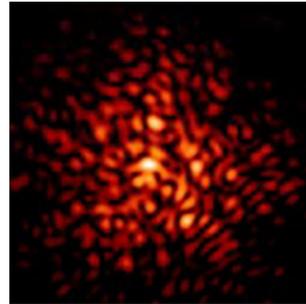


$$\rightarrow \left| \left| \leftarrow \lambda / D \right. \right.$$

Resolution limited by diffraction



On ground



$$\leftarrow \lambda / r_0 \rightarrow$$

Resolution Limited by turbulence

Image OL

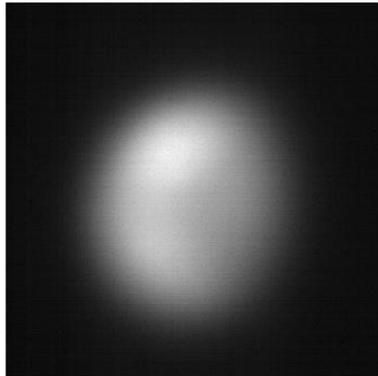
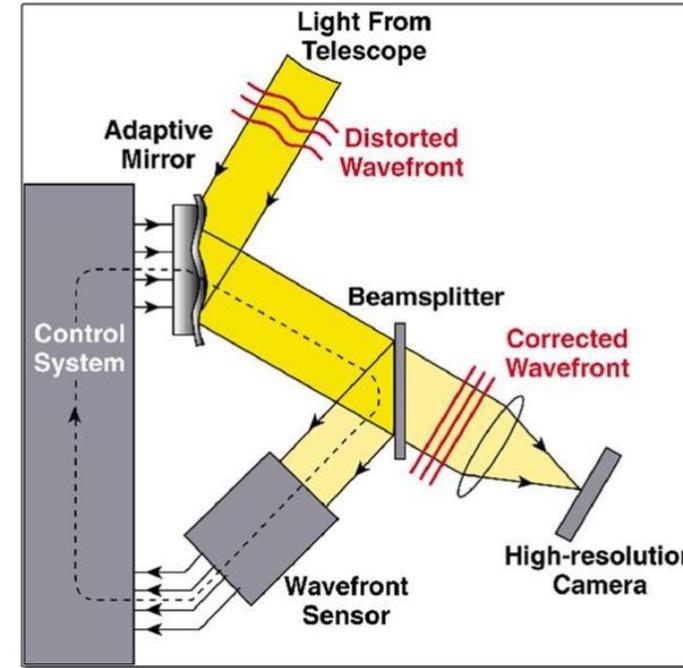
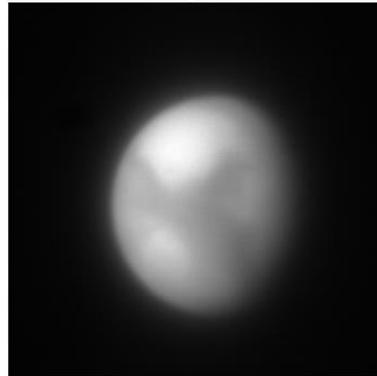


Image CL

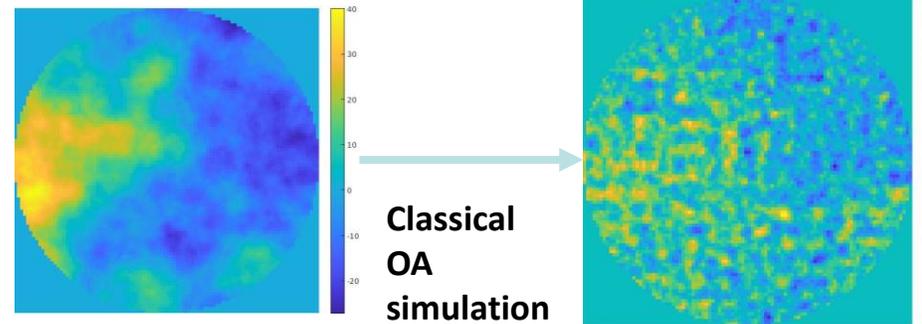


3 Main components

Wavefront sensor

Control system (real time computer)

Deformable mirror



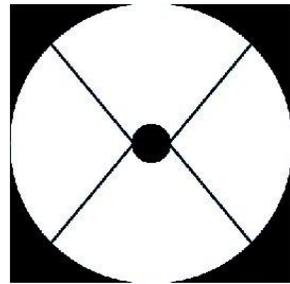
Classical OA simulation

Limited by :

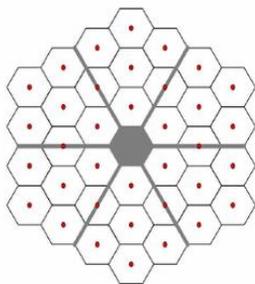
- number of DM actuator
- Control loop speed
- Wavefront sensor reconstruction

Credit : Romain Fétick → PAPHYRUS bench presentation Friday at 11:00

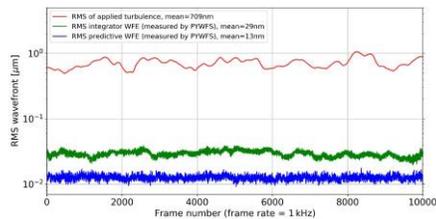
Adaptive Optics for giant telescope



Pupil VLT spider=5cm

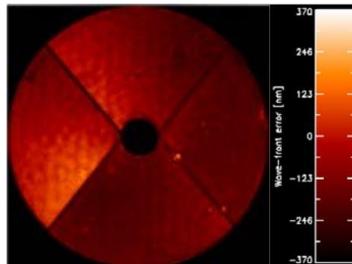


Pupil Keck spider=2,5cm

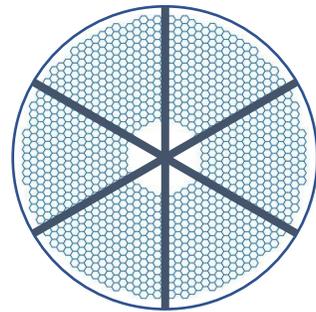


Credit : Rebecca Jensen-Clem

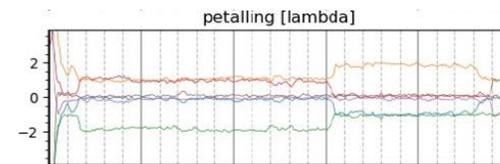
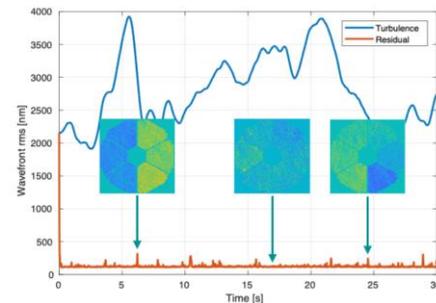
10m telescope (almost) not a problem for AO



Credit : Jean François Sauvage

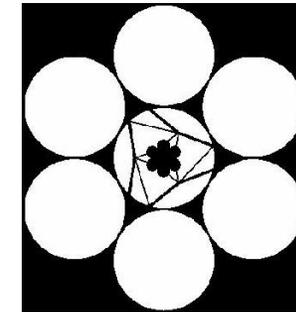
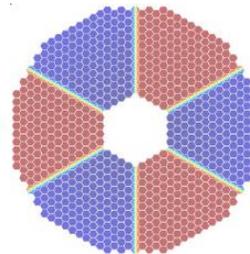


Pupil ELT Spider = 50cm

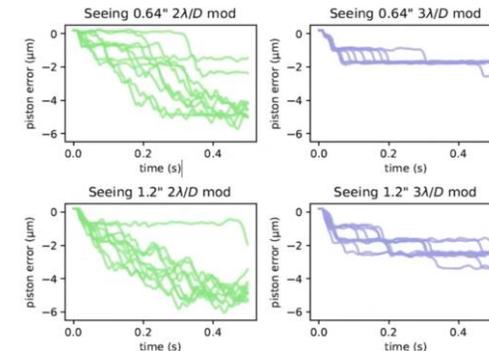


Credit : Charlotte Bond

30m class → telescopes becomes a major problem



Pupil GMT Spider >40cm

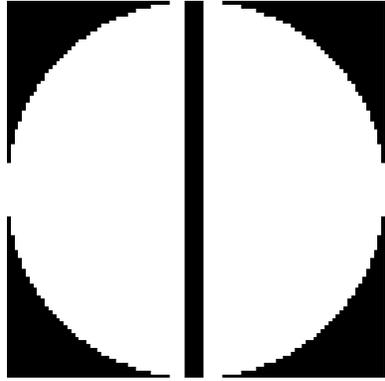


Credit : Sebastian Haffert

New challenge for wavefront reconstruction and control: phase gap → differential piston between pupil fragment → PSF limited by $D_{fragment}$

Our aim : reaching diffraction limit with a visible wavefront sensor

Modelisation of the problem : the toymodel



Toymodel pupil

Only 2 fragment, 1 petal mode

Test setting : ELT size spider (50cm) on a VLT-class telescope(10m)
Spider represents 5% of pupil diameter

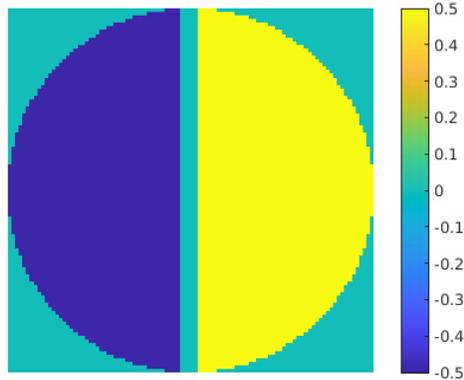


AO end to end loop
with fullpupil :

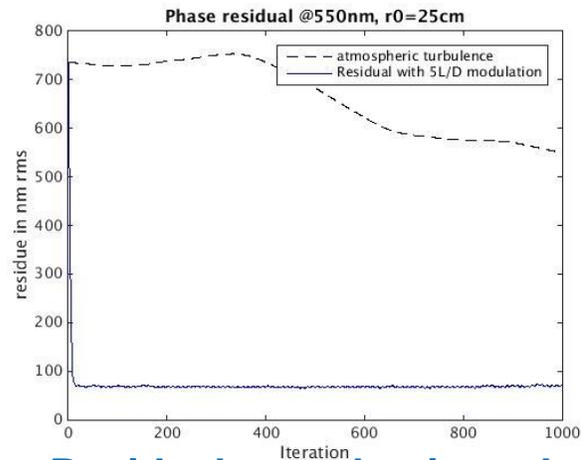


AO end to end loop
with spider in the
pupil :

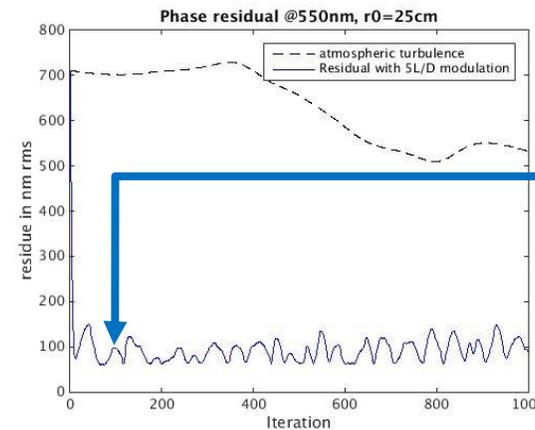
Conditions :
20*20 DM
D=10m
 $r_0=25\text{cm}$ @550nm
Wind speed=5m/s
No detector noise,
No sensor noise,
Sensing at $\lambda = 550\text{nm}$
F=500Hz
Spider size= 50cm
5 λ /D pyramid for control



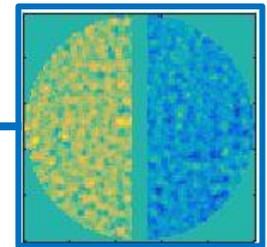
Petal mode



Residuals are dominated
by fitting error

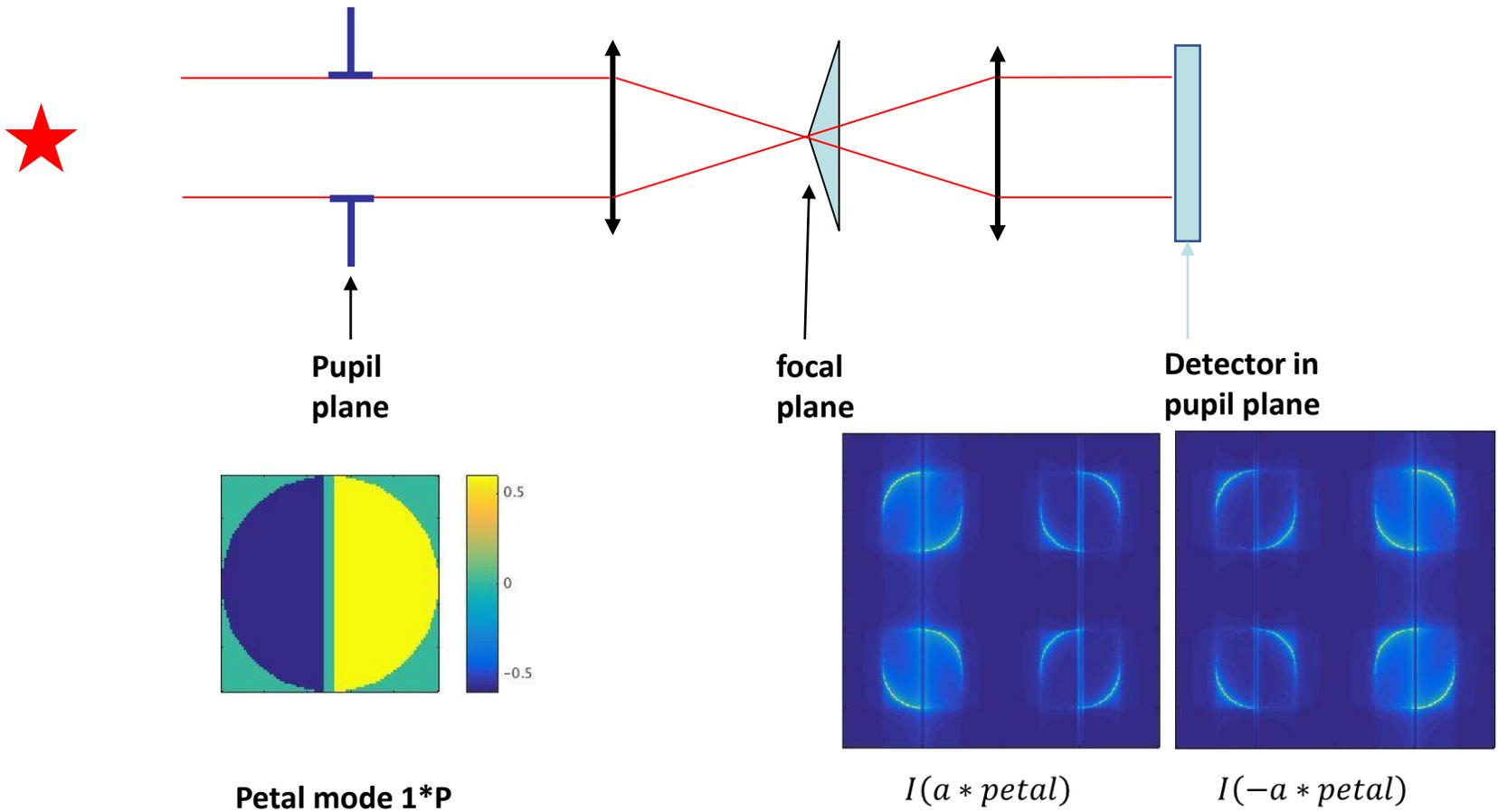


Residuals are fitting error
+ petal mode

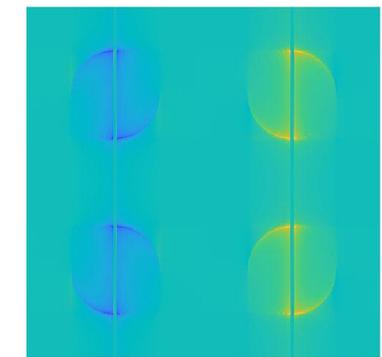


Phasescreens at
iteration 132

Pyramid wavefront sensor



$$\delta I(\varphi) = \frac{I(a * \varphi) - I(-a * \varphi)}{2 * a * F}$$

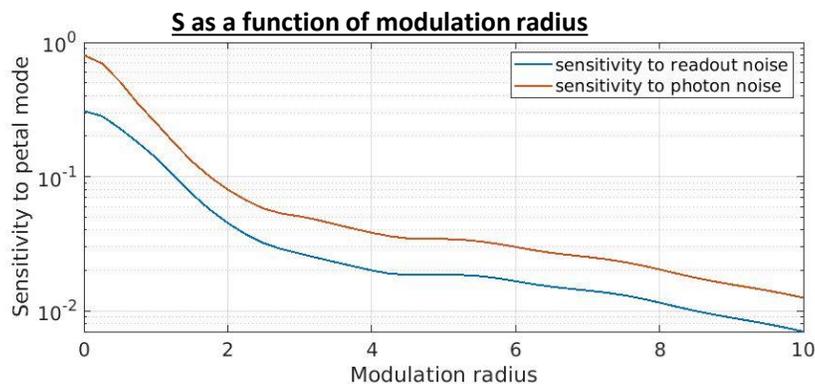
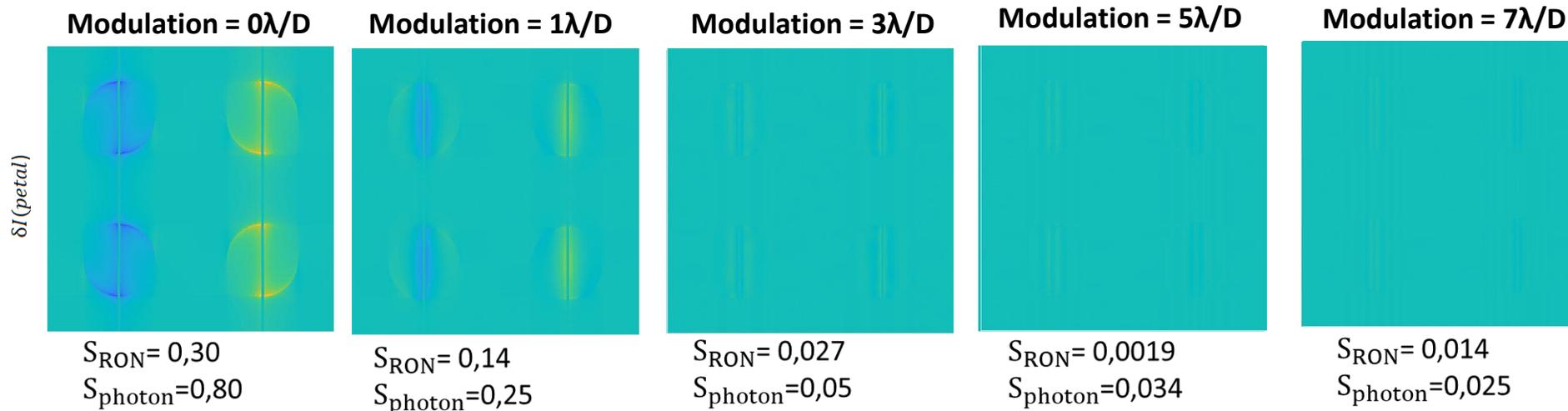


Flux $F = \sum_{\text{all pixels on detector}} I(0)$

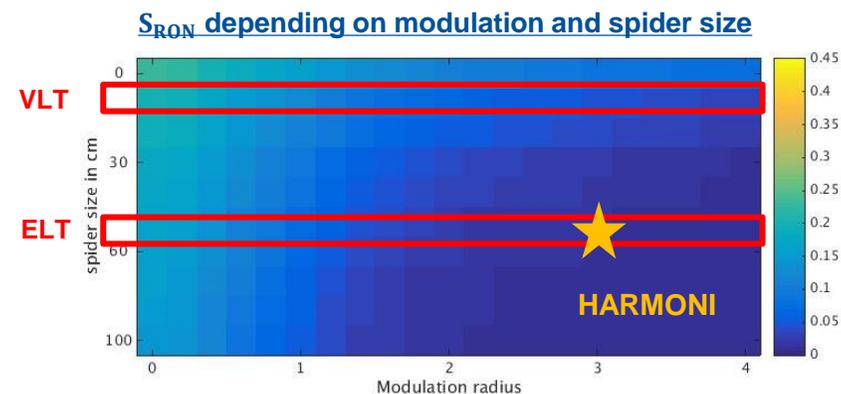
Ref : R. Ragazzoni 1996 'Pupil plane wavefront sensing with an oscillating prism'

Pyramid response to petal mode

Measure of sensitivity to petal mode : $S_{RON}(petal) = \|\delta I(petal)\|_2$ and $S_{photon}(petal) = \left\| \frac{\delta I(petal)}{\sqrt{I_0}} \right\|_2$



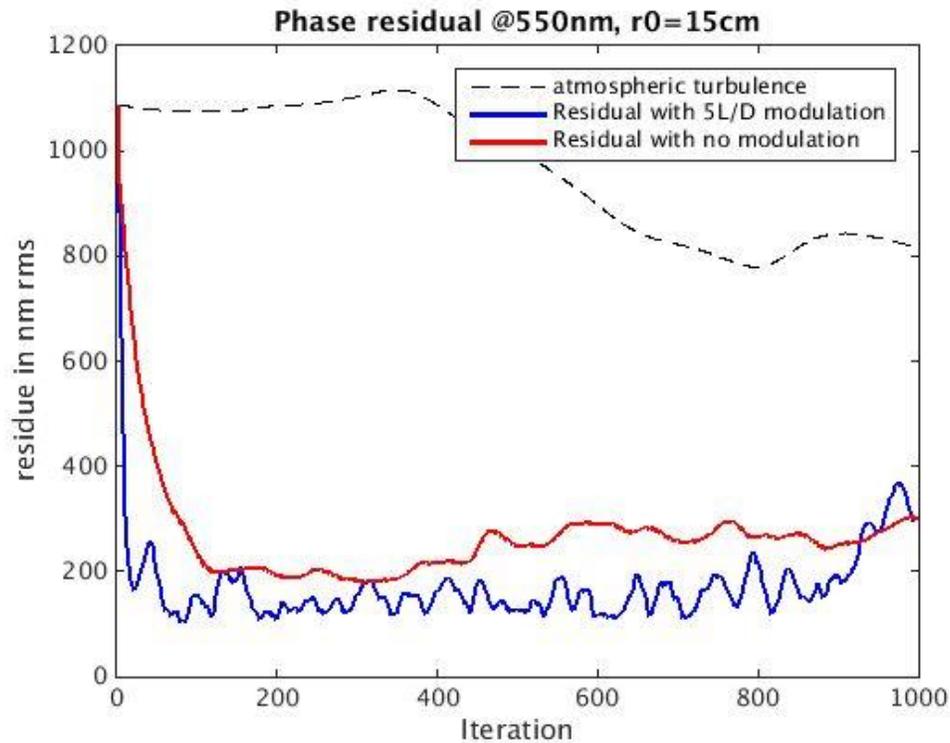
measure petal =
unmodulated pyramid



Ref : V.Chambouleyron 2022 'Optimizing Fourier-Filtering WFS to reach sensitivity close to the fundamental limit'

Pyramid control without modulation

Conditions :
20*20 DM
D=10m
 $r_0 = 15\text{cm}$ @550nm
Wind speed=5m/s
No detector noise,
No sensor noise,
Sensing at $\lambda = 550\text{nm}$
F=500Hz
Spider size= 50cm



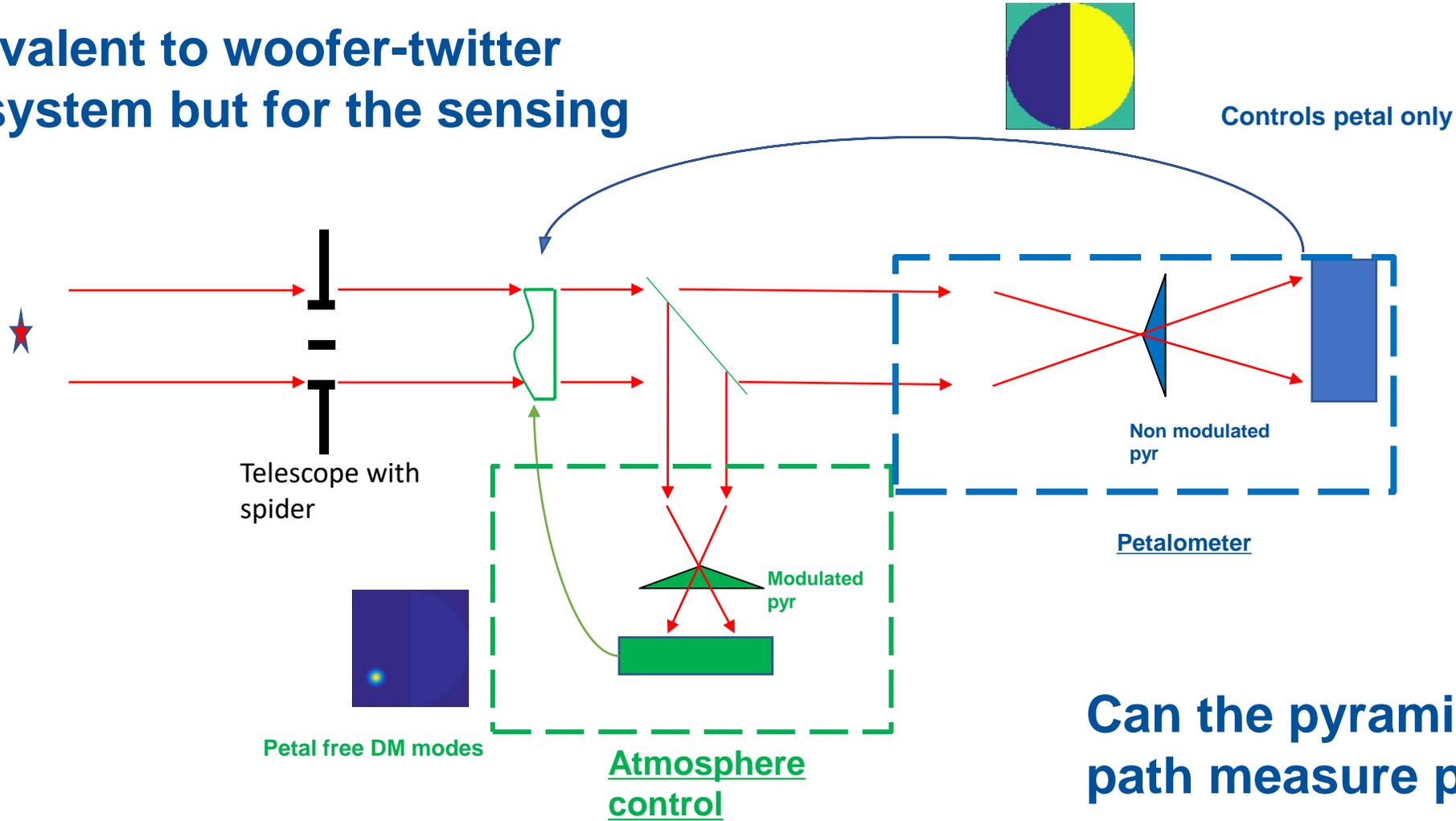
strong turbulence \rightarrow need modulation \rightarrow
not sensitive to piston

Petal when modulating better than no
modulation

Need two sensors,
1 for atmosphere
1 Petalometer

2 Path wavefront sensor

Equivalent to woofer-tweeter
AO system but for the sensing



Can the pyramid in second path measure petal ?

Petal estimation

$$D = [\delta I(\varphi_1); \delta I(\varphi_2); \delta I(\varphi_3) \dots]$$

$[\varphi_1, \varphi_2, \dots] = \text{Petal} + 29 \text{ first Zernike}$

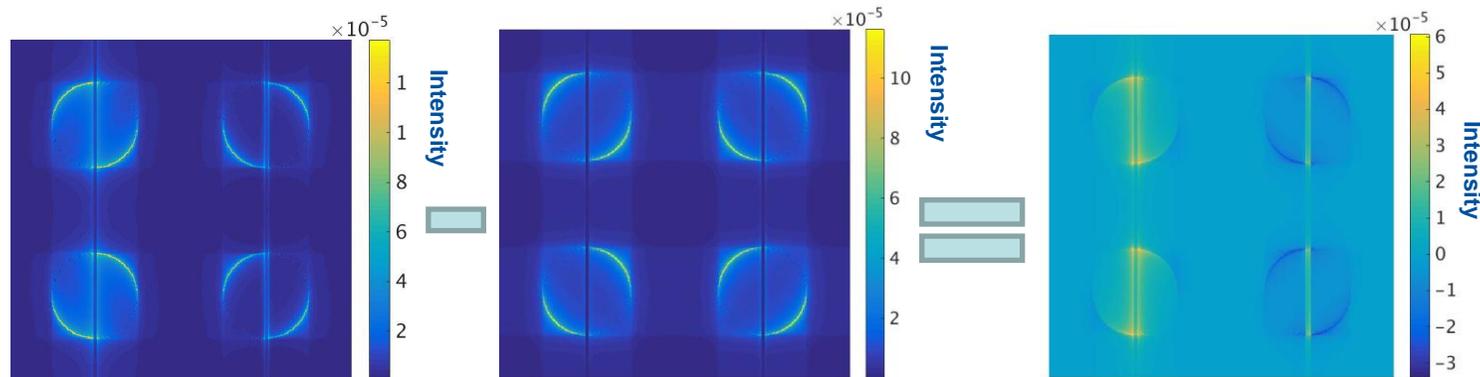
D : interaction matrix

D^\dagger : Reconstruction or control matrix

$$\Delta I(\varphi) = \frac{I(\varphi) - I(0)}{F}$$

$$\hat{p}(\varphi) = D^\dagger \times \Delta I(\varphi)$$

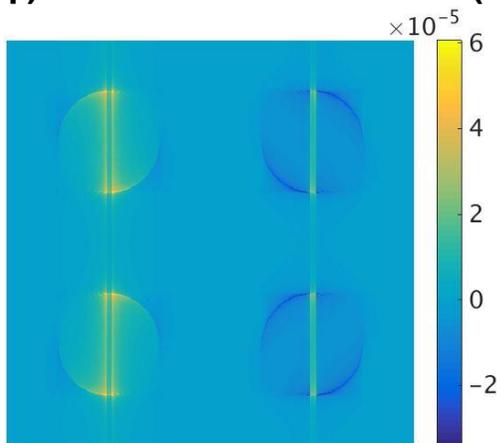
\hat{p} Reconstructed petal



$I(\varphi)/F$

$I(0)/F$

$\Delta I(\varphi)$



Introduced $p = -0.1 \text{ rad}$
 Reconstructed $\hat{p} = -0.1 \text{ rad}$

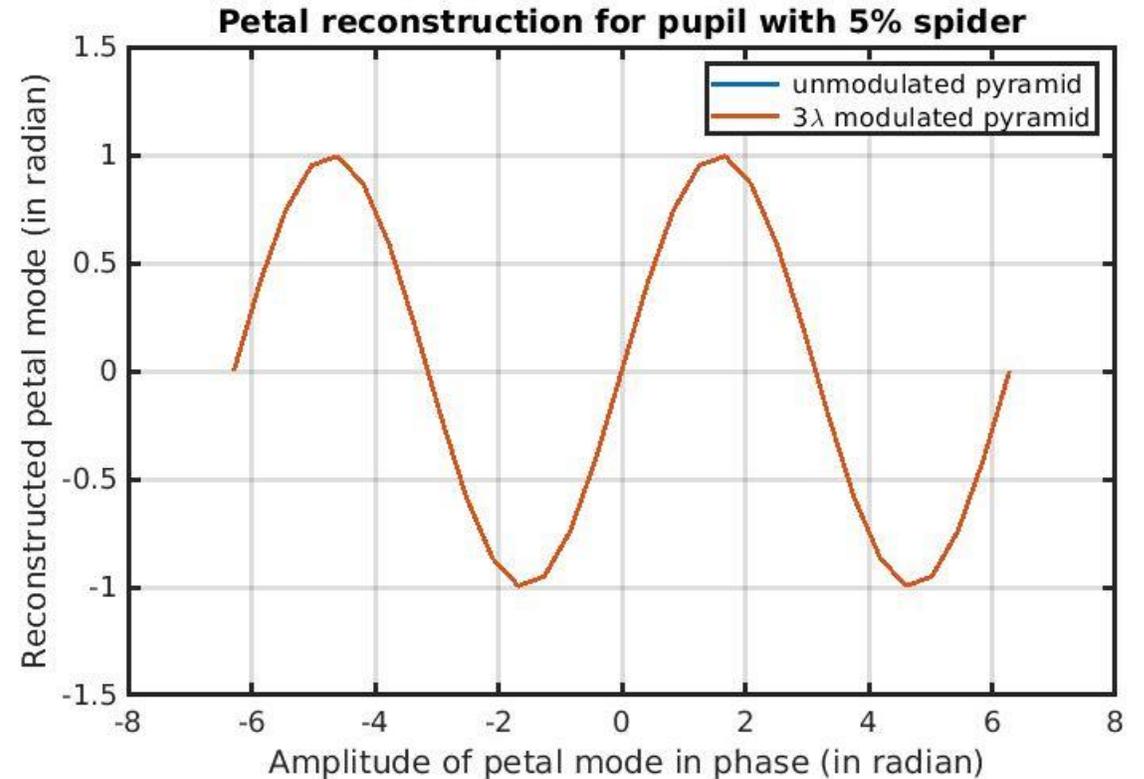
Goal : test \hat{p} VS p in presence of residuals

Petal reconstruction : with no atmosphere

Estimate \hat{p} for each $p \in [-2\pi, 2\pi]$

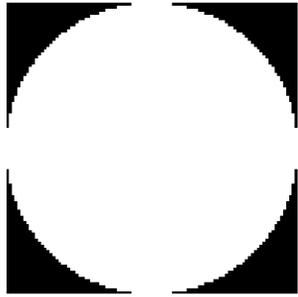
As expected, $\hat{p} = \sin(p)$

True for modulated and non modulated pyramid

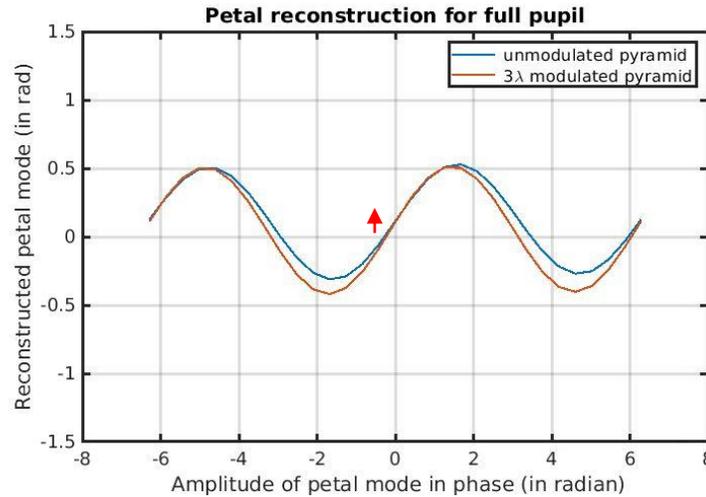


Linearity curve in absence of noise or atmosphere

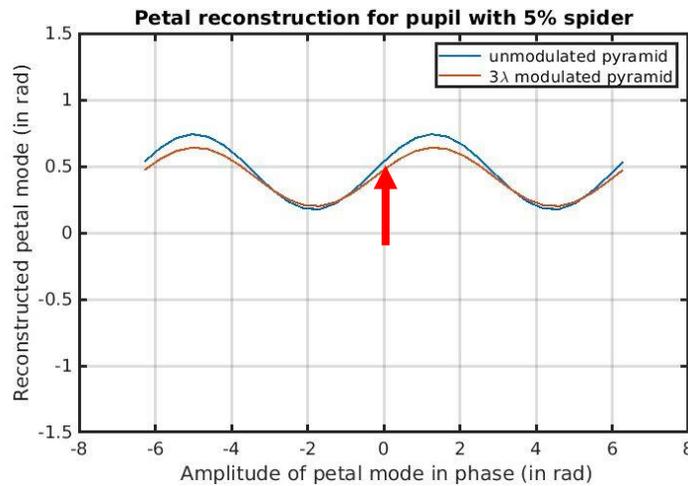
Petal reconstruction with 20x20 first stage residuals



fullpupil



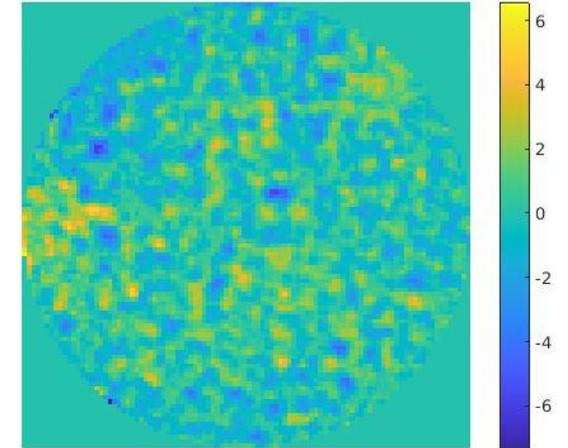
5% spider



Bias no modulation = 0.45 rad

Bias modulation = 0.42 rad

Residuals phase screen used :



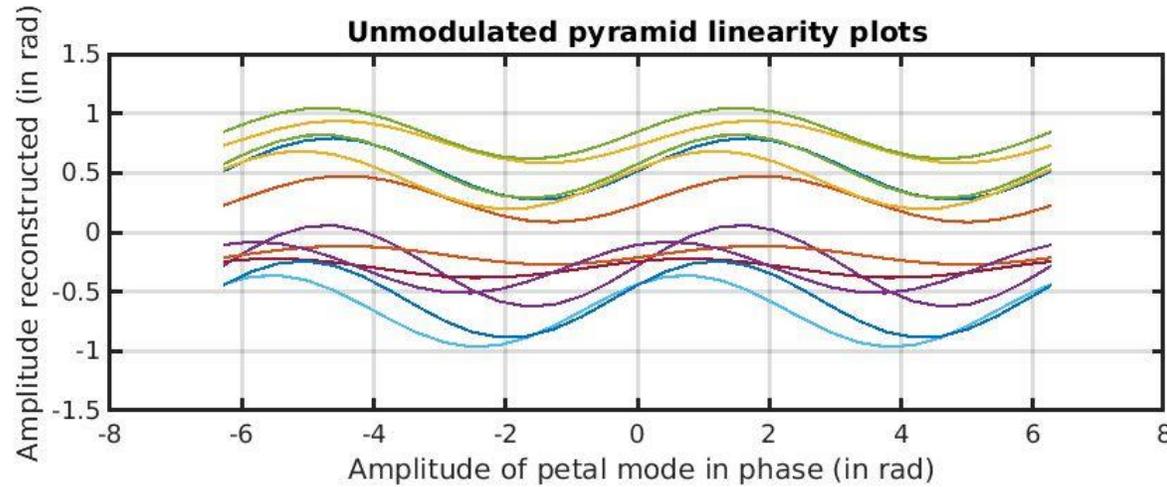
Conditions :
 20*20 DM
 D=10m
 $r_0=15\text{cm}$ @550nm
 Wind speed=5m/s
 No detector noise,
 No sensor noise,
 Sensing at $\lambda = 550\text{nm}$
 F=500Hz
 Spider size= 50cm
 Residual piston subtracted
 from phasescreen

Bias > min of reconstruction
 → cannot reconstruct 0

Petal reconstruction is biased in presence of residuals and spider

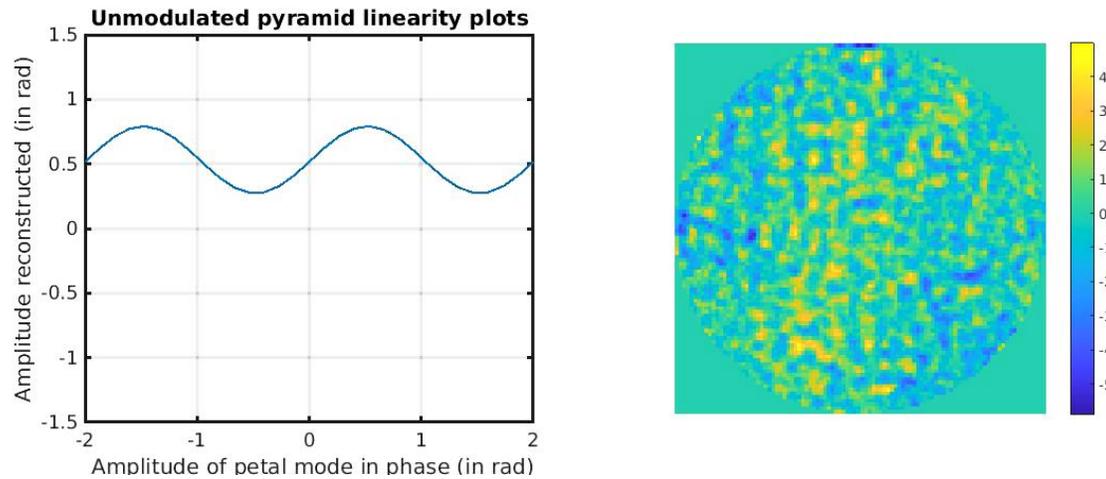
Petal reconstruction with variable residuals

Reconstruction made for
10 independant residuals



Bias not repeatable

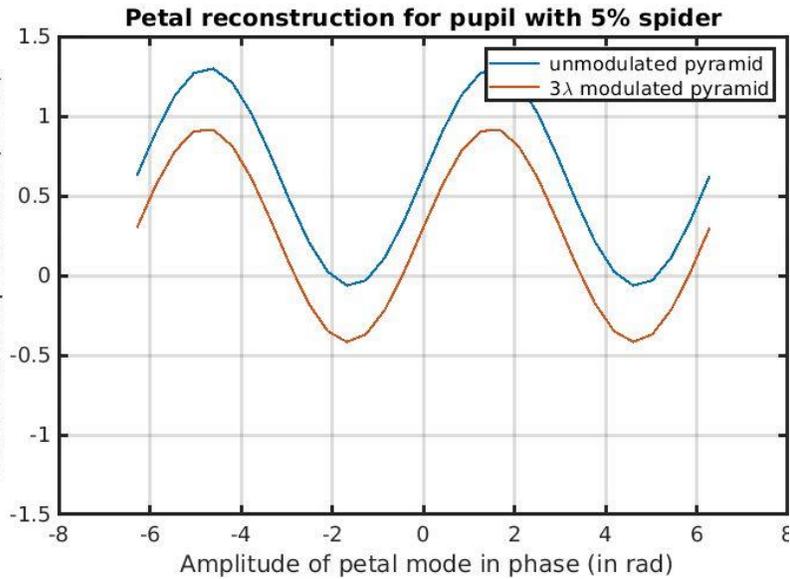
100 consecutive residual
phasescreens



Highly depedant on phase residuals
Fast evolving

Petal reconstruction with variable residuals

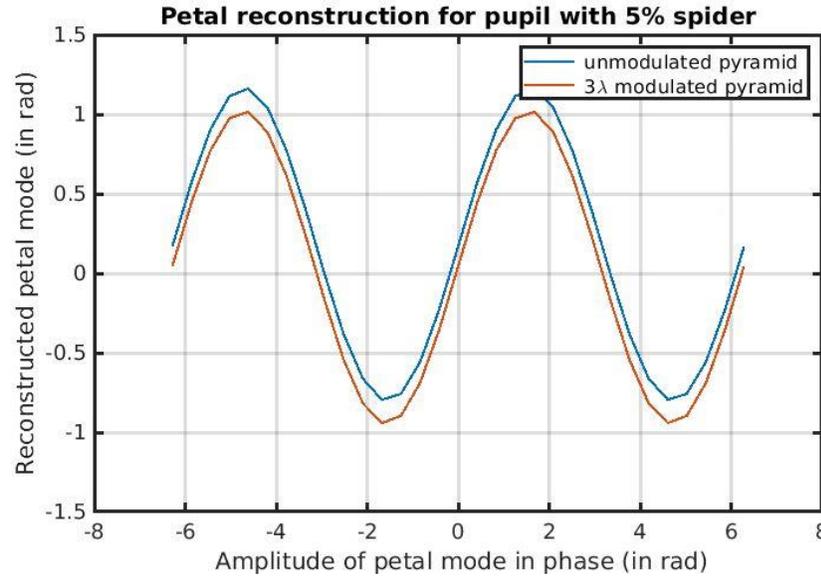
Residuals scaled by 0.5



Bias no modulation = 0.62 rad

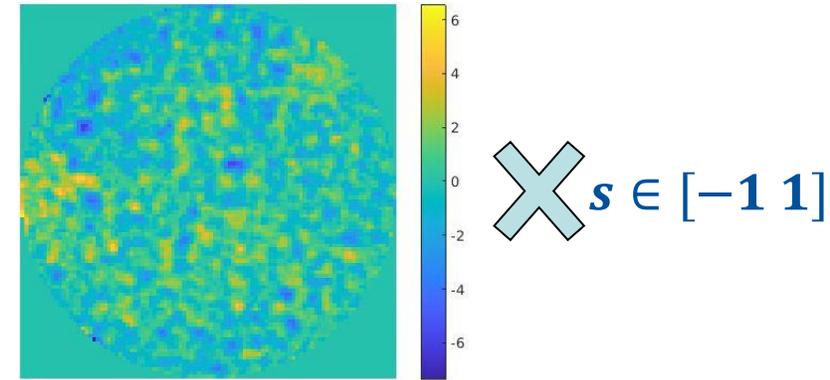
Bias modulation = 0.26 rad

Residuals scaled by 0.1

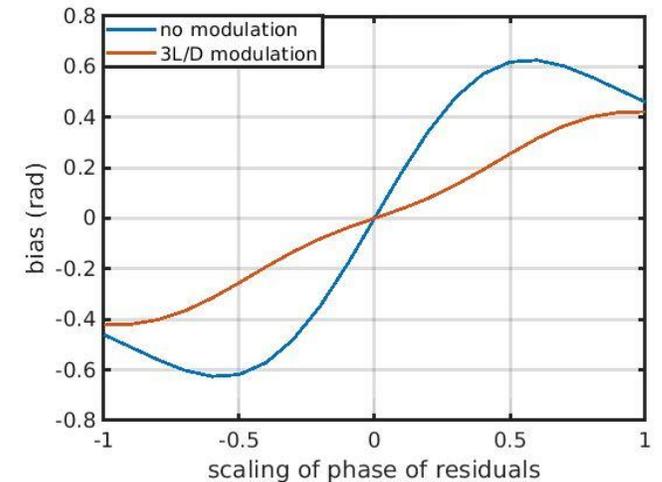


Bias no modulation = 0.18 rad

Bias modulation = 0.20 rad



Petal bias for different scaling of residual phase

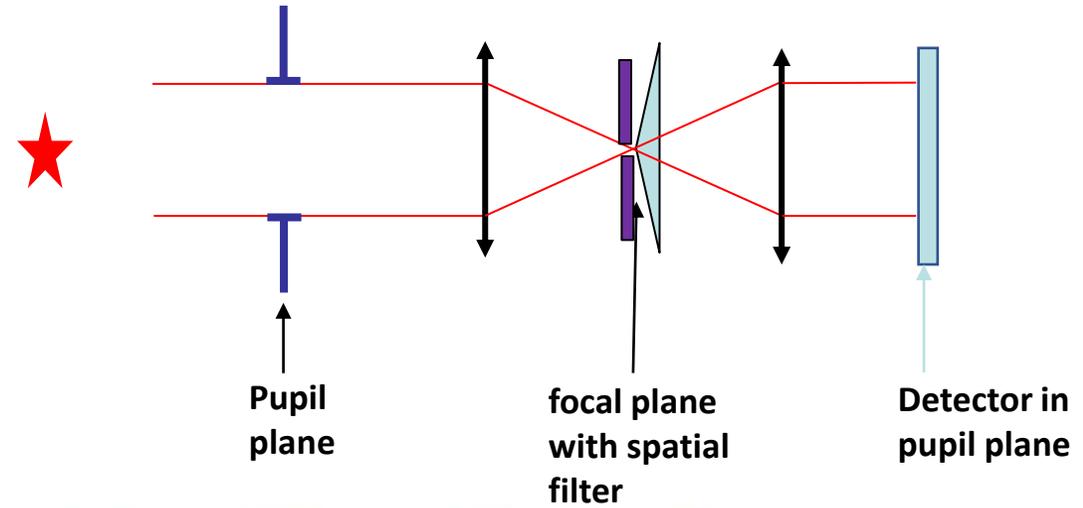


Bias is residual dependant → can't be controlled

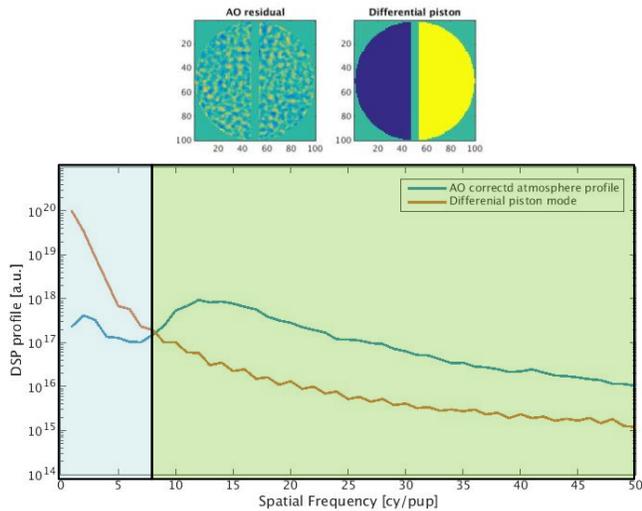
Reduce impact of residuals

Reduce the phase to be sensed → go to longer wavelength

Reduce impact of residuals → spatial filter in the focal plane



Petal dominates



Residual dominates

Spatial Filter Radius

15 λ/D

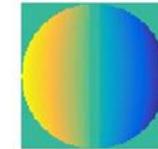
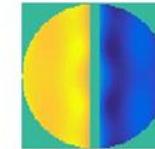
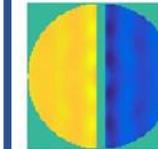
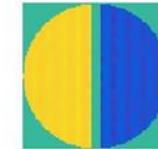
10 λ/D

5 λ/D

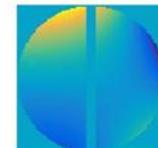
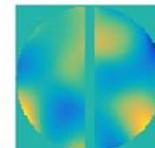
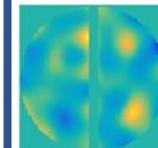
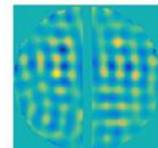
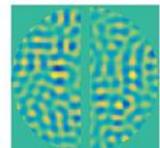
3 λ/D

1 λ/D

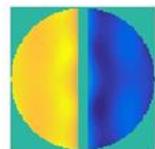
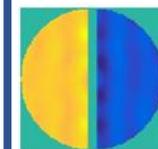
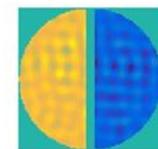
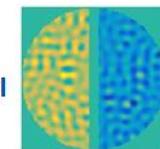
Piston



Atmospheric residual

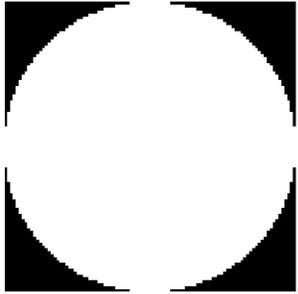


Atmospheric residual + Petal

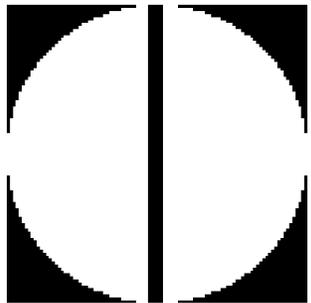
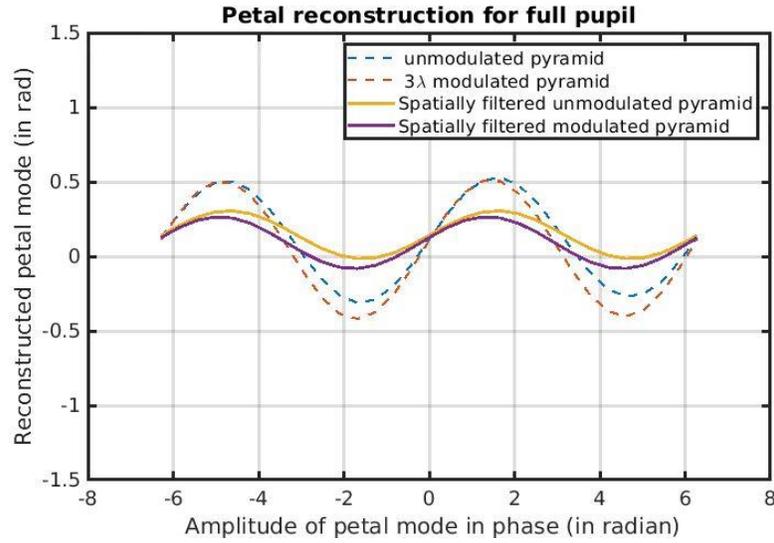


5 λ/D seems best compromise here

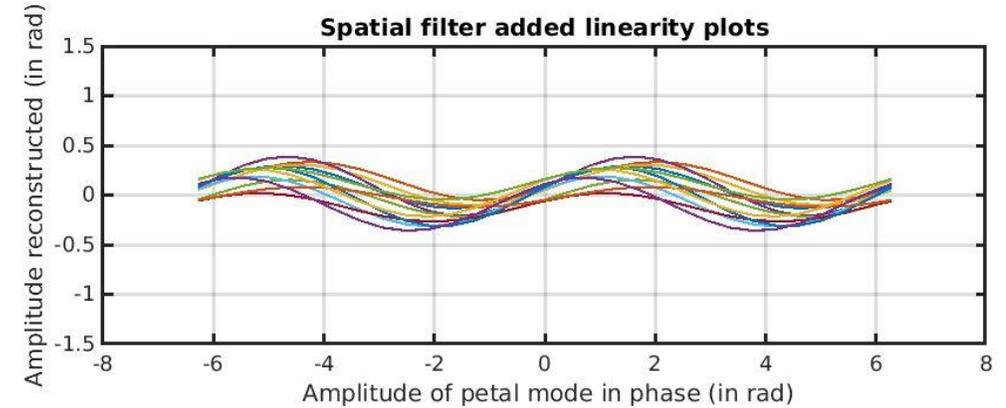
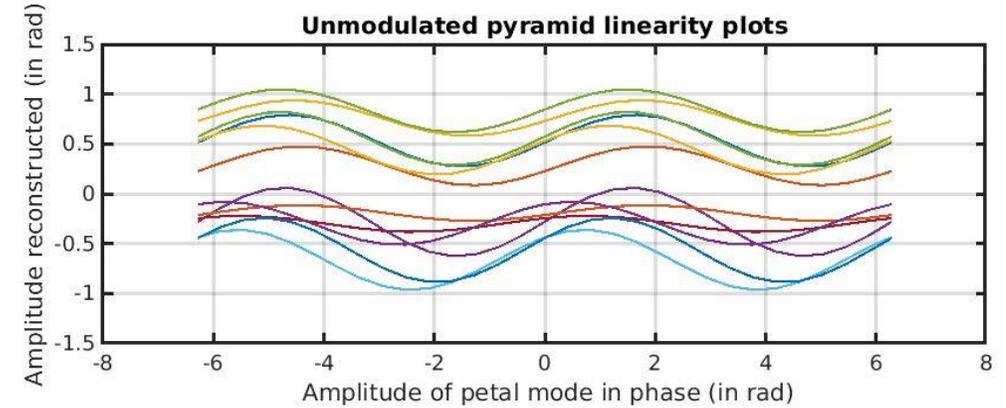
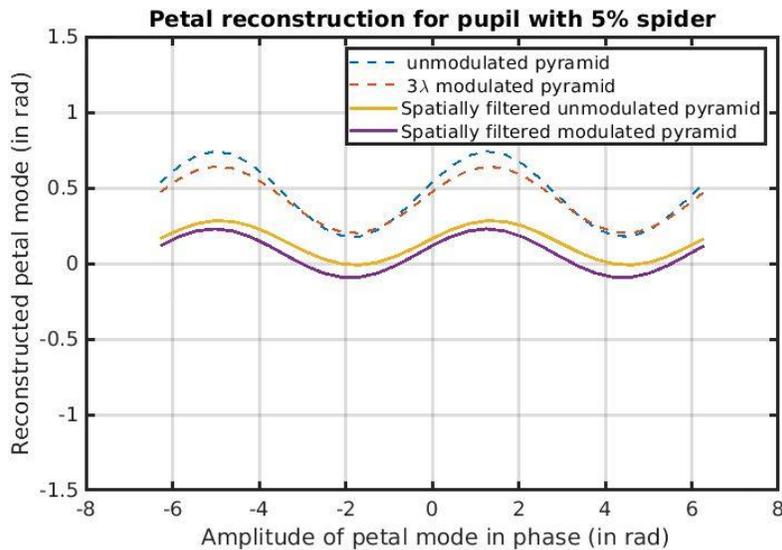
After spatial filtering linearity plots



fullpupil



5% spider



Spatially filtered reconstruction is the same with or without spider
→ Bias greatly reduced

Conclusion

- 2 sensor-system necessary to measure petal
- Residuals bias the petal measurement
- Spatial filter reduces this bias

Perspectives

Understanding origin of the bias → what creates bias in the residuals ?

Closed loop simulation → loss of light ? Size of spatial filter ? Best sensor ?

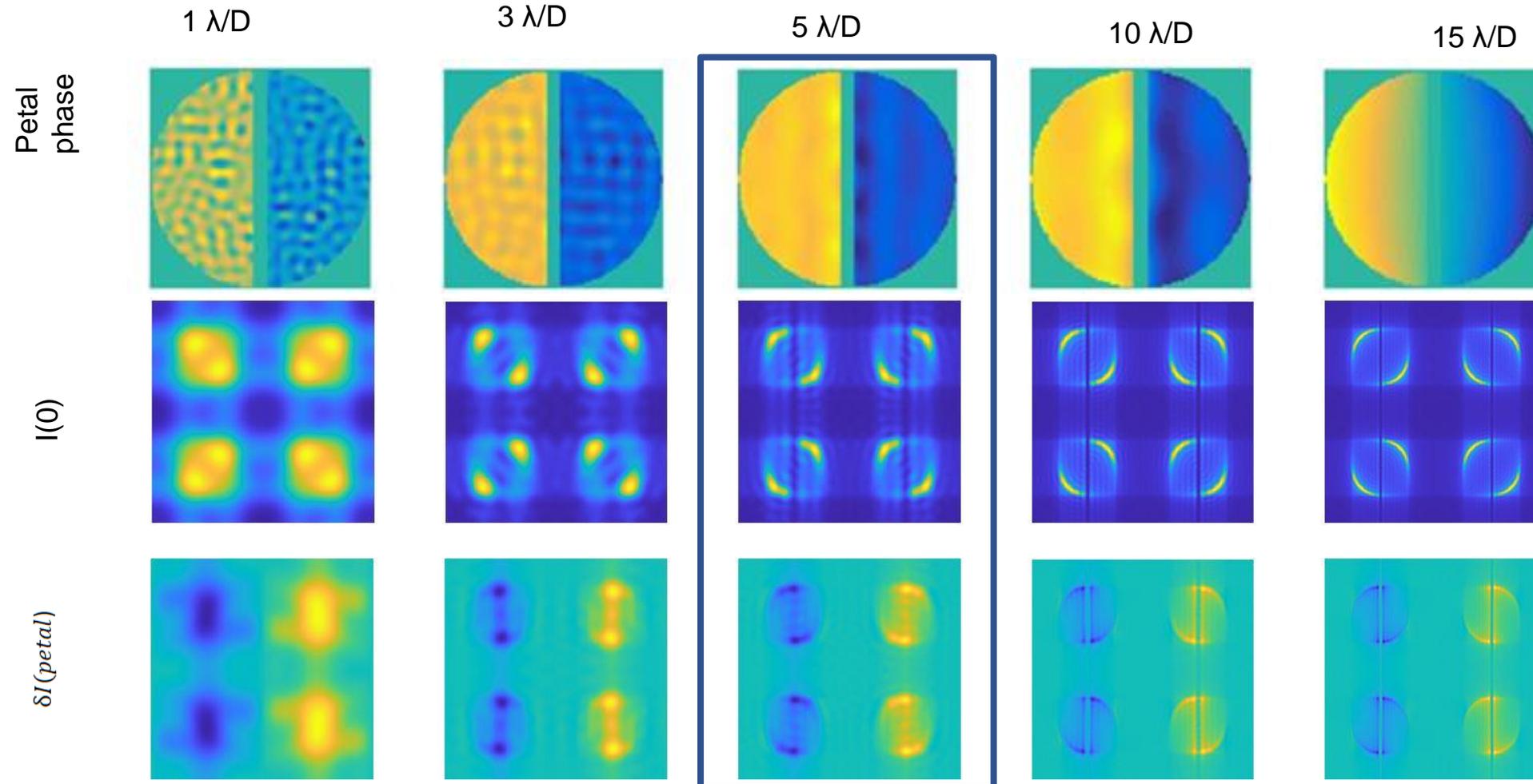
Simulation of ELT case

Spatial filter interest for other Fourier Filtering WFS

Test on PAPHYRUS ?

Thank you for listening !

Annex : Spatial filter effect on pyramid signal

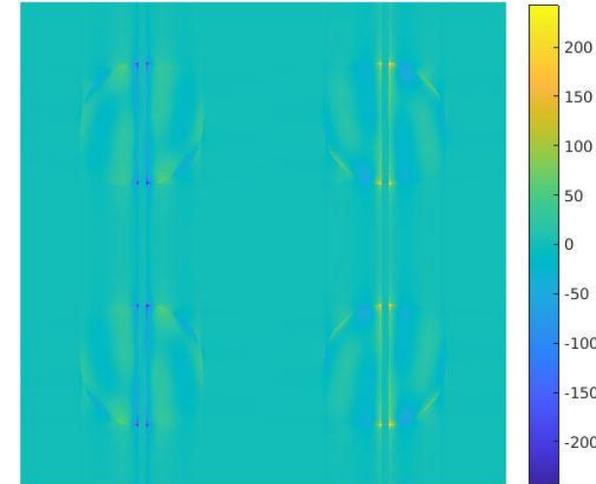


5 λ/D seems best compromise here

Annex Origin of the bias

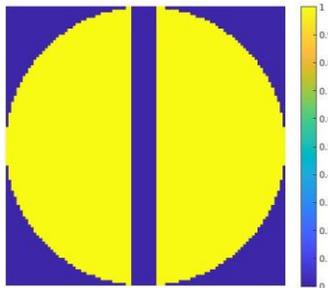
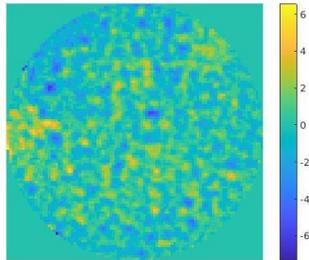
D^\dagger of petal

Look at $D^\dagger \rightarrow$ what signal is used for petal reconstruction



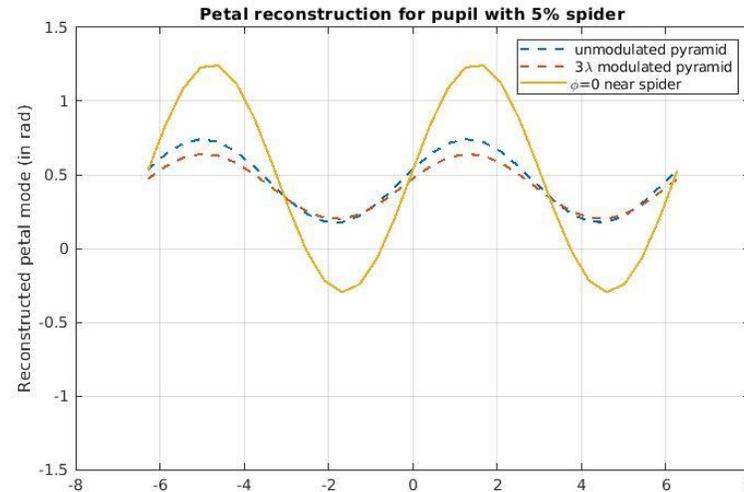
Signal of petal reconstruction very close to spider \rightarrow Residual next to spider causing bias ?

Blunt test : zero phase next to spider



Phase screen

As if Spider = 90cm

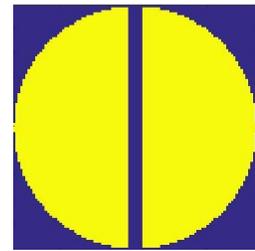


No effect on bias !

Origin of bias not understood

Comes from phase residuals

Annex : Improving sensitivity to petal



Toymodel pupil

No Spider

Spider

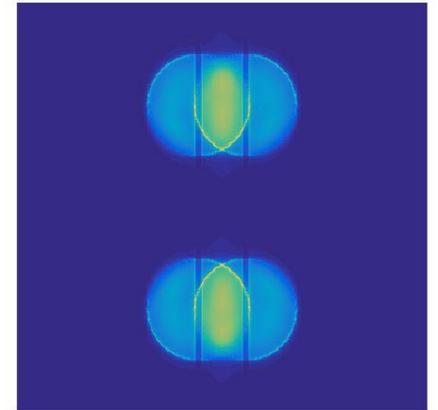
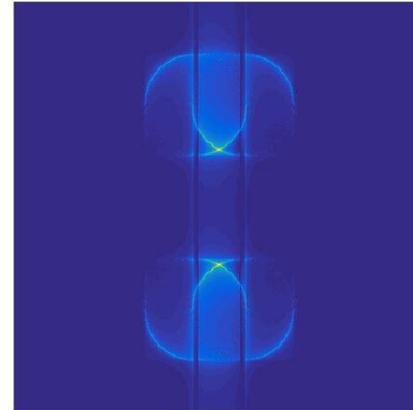
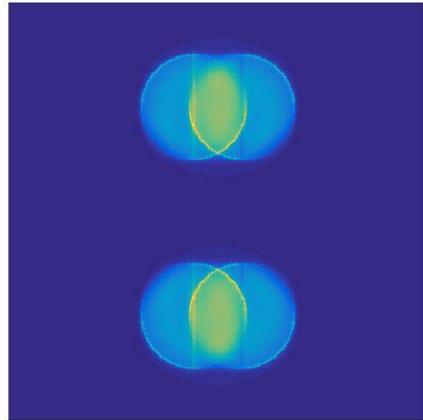
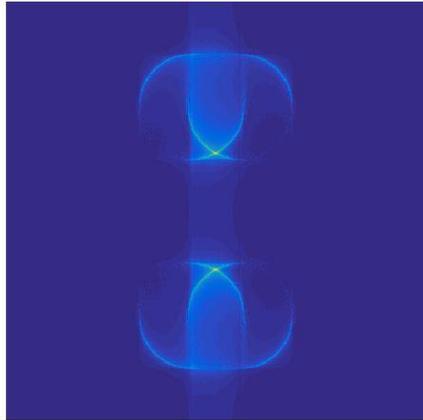
No modulation

3 λ/D modulation

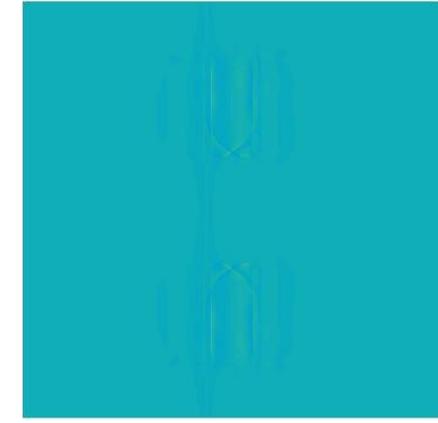
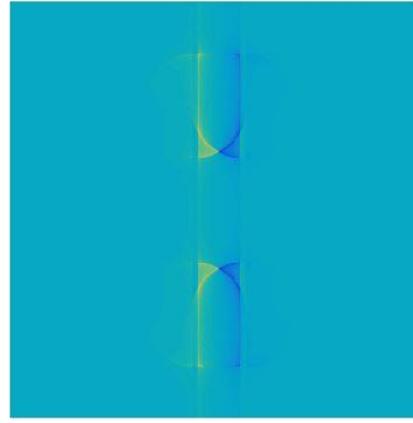
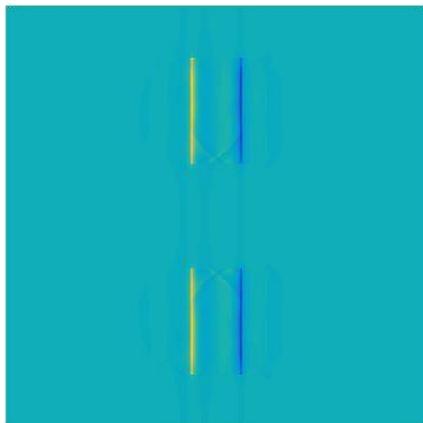
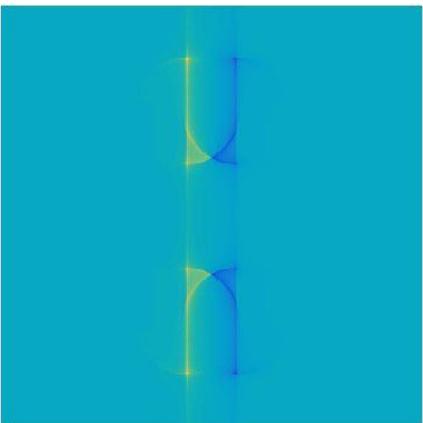
No modulation

3 λ/D modulation

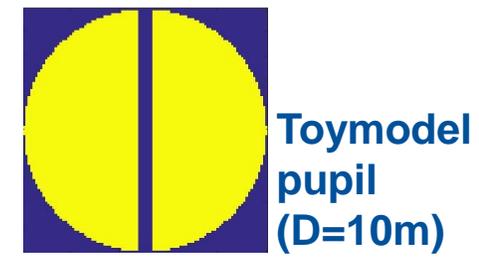
I ref



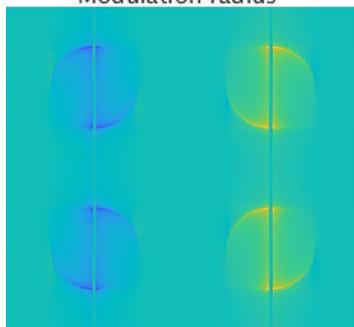
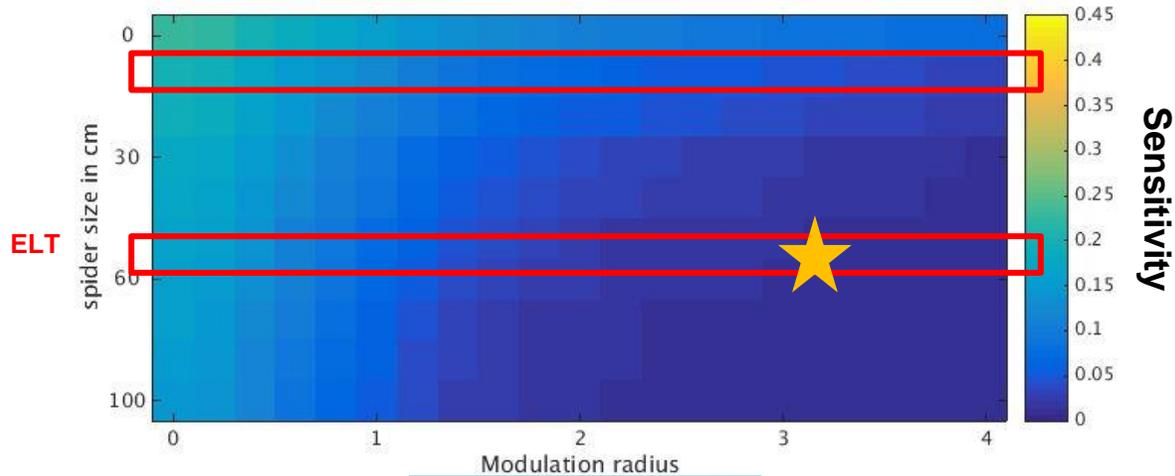
I piston



II Improving sensitivity to Petal : Loss with spider when modulating



classic 4 sided pyramid



Asymmetric pyramid

